

1. Use sum and difference formulas to simplify each expression.

A.  $\sin 42^\circ \cos 17^\circ - \cos 42^\circ \sin 17^\circ \quad \sin 25^\circ$

B.  $\cos 94^\circ \cos 18^\circ + \sin 94^\circ \sin 18^\circ \quad \cos 76^\circ$

C.  $\sin(\pi/5) \cos(\pi/2) + \sin(\pi/2) \cos(\pi/5) \quad \sin \frac{7\pi}{10}$

D.  $\sin 3x \cos x - \cos 3x \sin x \quad \sin 2x$

E.  $\frac{\tan 19^\circ + \tan 47^\circ}{1 - \tan 19^\circ \tan 47^\circ} \quad \tan 66^\circ$

F.  $\frac{\tan \frac{\pi}{5} - \tan \frac{\pi}{3}}{1 + \tan \frac{\pi}{5} \tan \frac{\pi}{3}} \quad \tan\left(-\frac{2\pi}{15}\right)$

2. Find the EXACT value of each expression.

A.  $\sin 105^\circ \quad \frac{\sqrt{6} + \sqrt{2}}{4}$

B.  $\cos\left(\frac{7\pi}{12}\right) \quad \frac{\sqrt{2} - \sqrt{6}}{4}$

C.  $\tan 15^\circ \quad \frac{\sqrt{3}-1}{1+\sqrt{3}} = -\sqrt{3} + 2$

D.  $\tan\left(\frac{11\pi}{12}\right)$

E.  $\sin\left(-\frac{\pi}{12}\right)$

$$\frac{-\sqrt{3}+1}{1+\sqrt{3}} = \sqrt{3}-2$$

$$\frac{-\sqrt{6}+\sqrt{2}}{4}$$

3. Prove:  $\frac{\sin(A+B)}{\cos A \cos B} = \tan A + \tan B$

$$\frac{\sin A \cos B + \cos A \sin B}{\cos A \cos B} \Rightarrow \frac{\sin A \cos B}{\cos A \cos B} + \frac{\cos A \sin B}{\cos A \cos B} \Rightarrow \tan A + \tan B$$

4. Prove:  $\sin(\pi + \theta) = -\sin \theta$

$$\begin{aligned} & \sin \pi \cos \theta + \cos \pi \sin \theta \\ & 0 \cdot \cos \theta + -1 \cdot \sin \theta \\ & -\sin \theta \end{aligned}$$

5. Prove:  $\tan(\pi - \theta) = -\tan \theta$

$$\frac{\tan \pi - \tan \theta}{1 + \tan \pi \tan \theta} \Rightarrow \frac{0 - \tan \theta}{1 + 0 \cdot \tan \theta} \Rightarrow -\frac{\tan \theta}{1} \Rightarrow -\tan \theta$$

6. Given  $\sin x = \frac{3}{5}$  for  $0 < x < \frac{\pi}{2}$  and  $\cos y = \frac{2}{\sqrt{5}}$  for  $-\frac{\pi}{2} < y < 0$ , find:

- a.  $\sin(x+y)$       b.  $\sin(x-y)$       c.  $\cos(x+y)$

$$\frac{2}{5\sqrt{5}} = \frac{2\sqrt{5}}{25}$$

$$\frac{2}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$$

$$\frac{11}{5\sqrt{5}} = \frac{11\sqrt{5}}{25}$$